RSHS SCHOOL Yr 11/12

MATHEMATICS 2C/2D
Section One:
Calculator-free

SOLUTIONS

Student Number: In figures

In words

Your name   MARKING KEY

Time allowed for this section
Reading time before commencing work: five minutes
Working time for this section: fifty minutes

Materials required/recommended for this section
To be provided by the supervisor
This Question/Answer Booklet
Formula Sheet

To be provided by the candidate
Standard items: pens, pencils, pencil sharpener, eraser, correction fluid/tape, ruler, highlighters

Special items: nil

Important note to candidates

No other items may be used in this section of the examination. It is **your** responsibility to ensure that you do not have any unauthorised notes or other items of a non-personal nature in the examination room. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

Structure of this paper

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of exam
Section One: Calculator-free	7	7	50	50	33
Section Two: Calculator-assumed	12	12	100	100	67
			Total	150	100

Instructions to candidates

1. The rules for the conduct of Western Australian external examinations are detailed in the *Year 12 Information Handbook 2012*. Sitting this examination implies that you agree to abide by these rules.

2. Write your answers in the spaces provided in this Question/Answer Booklet. Spare pages are included at the end of this booklet. They can be used for planning your responses and/or as additional space if required to continue an answer.
    *   Planning: If you use the spare pages for planning, indicate this clearly at the top of the page.
    *   Continuing an answer: If you need to use the space to continue an answer, indicate in the original answer space where the answer is continued, i.e. give the page number. Fill in the number of the question(s) that you are continuing to answer at the top of the page.

3. **Show all your working clearly**. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat an answer to any question, ensure that you cancel the answer you do not wish to have marked.

4. It is recommended that you **do not use pencil**, except in diagrams.

Section One: Calculator-free   **(50 Marks)**

This section has **seven (7)** questions. Answer **all** questions. Write your answers in the spaces provided.

Working time for this section is 50 minutes.

Question 1   **(7 marks)**

(a)   Simplify the expression $\dfrac{2^2 \times 5^5}{4 \times 5^3}$.   (2 marks)

$$= \frac{4}{4} \times 5^2 \quad \checkmark$$
$$= 25 \quad \checkmark$$

(b)   Find $f(3)$ if $f(x) = 2x^2 - 4x - 3$.   (1 mark)

$$= 2 \times 3^2 - 4 \times 3 - 3$$
$$= 18 - 12 - 3 \quad \checkmark$$
$$= 3$$

(c)   Factorise

       (i) $x^2 - x - 20$.   (1 mark)

$$(x + 4)(x - 5) \quad \checkmark$$

       (ii) $9x^2 - 4$.   (1 mark)

$$= (3x)^2 - (2)^2$$
$$= (3x + 2)(3x - 2) \quad \checkmark$$

(d)   Solve the equation $(3x - 2)(x + 5) = 0$ (2 marks)

$$3x - 2 = 0$$
$$x = \frac{2}{3} \quad \checkmark$$
$$\text{or}$$
$$x + 5 = 0 \quad \checkmark$$
$$x = -5$$

See next page

Question 2 **(7 marks)**

The coordinates of four points are A(2, -1), B(1, 2), C(0, 5) and D(4, 8).

(a) Determine the gradient of the Line 1, which passes through A and B. (2 marks)

$$m = \frac{(2) - (-1)}{(1) - (2)} \quad \checkmark$$
$$m = \frac{3}{-1}$$
$$m = -3 \quad \checkmark$$

(b) Line 2 passes through point C and has a gradient of $\frac{1}{3}$.

Write down the equation of this line. (1 mark)

$$y = \frac{1}{3}x + 5 \quad \checkmark$$

(c) Explain whether Line 1 and Line 2 are parallel, perpendicular or neither. (2 marks)

Perpendicular, as the product of the gradients of these lines is $-3 \times \frac{1}{3} = -1$ $\checkmark$ $\checkmark$

(d) Calculate the distance between points C and D, if one unit is one centimetre. (2 marks)

$$d = \sqrt{(4-0)^2 + (8-5)^2} \quad \checkmark$$
$$d = \sqrt{16 + 9}$$
$$d = \sqrt{25}$$
$$d = 5 \text{ cm} \quad \checkmark$$

Question 3 (8 marks)

In a random survey of 100 swimmers at a council owned pool, three-quarters said they swam regularly. 35 males said they swam regularly and 10 more males than females were surveyed.

(a) If one of the swimmers surveyed was chosen at random, what is the probability that they did not swim regularly? (1 mark)

$$1 - \frac{3}{4} = \frac{1}{4}$$ ✓

(b) Complete this two-way table using the above information. (3 marks)

	Swam regularly	Did not swim regularly	Total	
Female	40	5	45	✓
Male	35	20	55	✓ per line
Total	75	25	100	✓

(c) If one of those surveyed said they did not swim regularly, are they more likely to be female or male? Justify your answer. (2 mark)

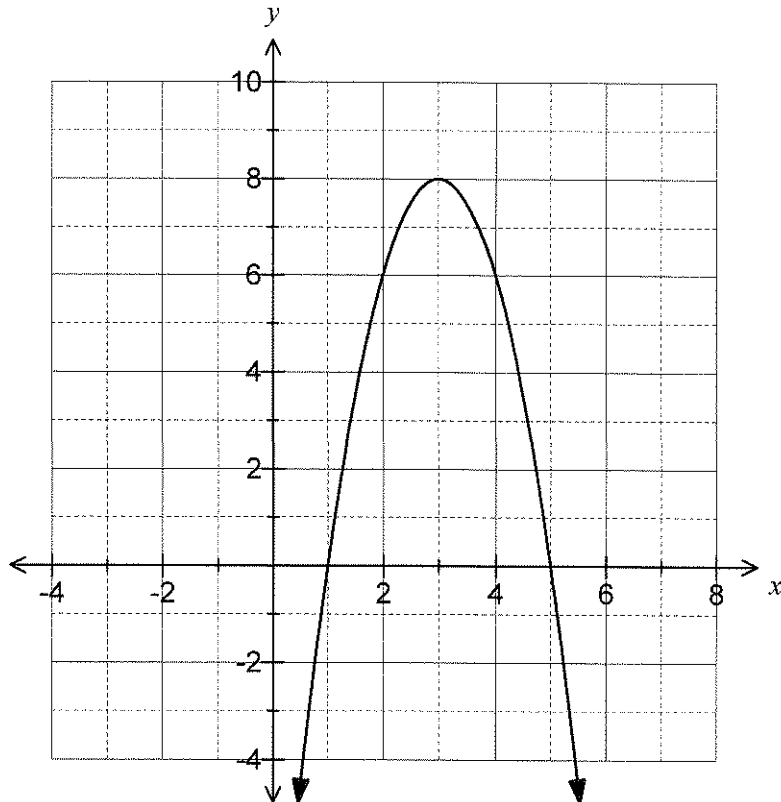Male since $\frac{20}{25} > \frac{5}{25}$ ✓ ✓

follow through

(d) If only 25 swimmers had been surveyed, how many of these would you expect to be males who say that they swam regularly? (2 mark)

$$\frac{1}{4} \times 35 \approx 9 \text{ males}$$ ✓ ✓

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Question 4 (9 marks)

(a) The graph of $y = -2(x-3)^2 + 8$ is drawn below.

For this graph, determine

(i) the equation of the line of symmetry (1 mark)

$$x = 3$$ ✓

(ii) the coordinates of the turning point (1 mark)

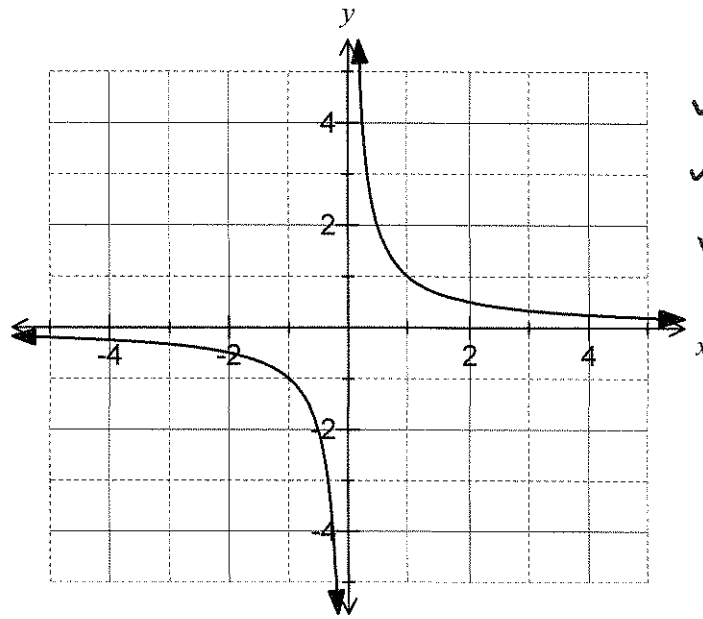$$(3, 8)$$ ✓

(iii) the coordinates of the y-intercept (1 mark)

$$-2(-3)^2 + 8 = -10$$
$$\therefore (0, -10)$$ ✓ must be as coordinates

(iv) the equation of the graph in the form $y = -2(x-a)(x-b)$, where a and b are integers. (1 mark)

$$y = -2(x-1)(x-5)$$ ✓

(b) Draw the graph of $y = \dfrac{1}{x}$ on the axes below. (3 marks)

✓ shape
✓ two sections
✓ Axes as asymptotes

(c) Two of the functions $y = 2^x$, $y = x^3$ and $y = x^2$ were used to create Table A and Table B below. On the line below each table, write the function used. (2 marks)

x	0	1	2
y	0	1	8

Table A

x	0	1	2
y	1	2	4

Table B

$y = x^3$ ✓

$y = 2^x$ ✓

See next page

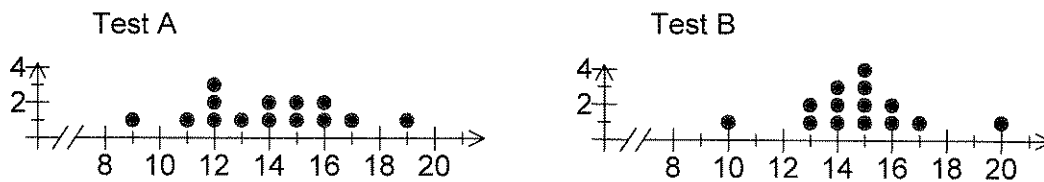**Question 5**   **(7 marks)**

A class sat two tests and the scores of the students in each are shown below.

Test A   Test B

(a)   The mean score was 13.9 for Test A. Is the mean of scores in Test B larger than, smaller
       than, or equal to 13.9? Explain your answer.   (2 marks)

> Larger. ✓
>
> In Test B, only 3 scores were below 13.9, with 11 above. ✓
> Also, most scores were clustered around 15.

(b)   What is the range of scores in Test A?   (1 mark)

> 10   ✓

(c)   The standard deviation of scores in Test A was 2.18. Is the standard deviation of scores in
       Test B larger than, smaller than, or equal to 2.18? Explain your answer.   (2 marks)

> Smaller. ✓
>
> Scores in Test B are clustered more tightly together than
> those in Test A. ✓

(d)   Which is the better measure to compare the spread of scores in these two tests – the
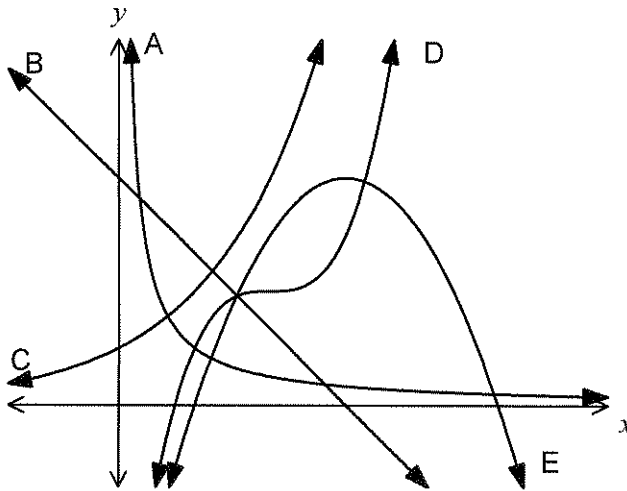   range or the standard deviation? Justify your choice.   (2 marks)

> Standard deviation. ✓
>
> The range is the same for both tests, yet it can be seen that
> the spreads are different, reflected in the smaller standard
> deviation for Test B. ✓

Question 6 (6 marks)

The graphs (A, B, C, D and E) and equations (P, Q, R, S and T) of five functions are shown below.

P $y = 2^x$

Q $y = -(x-3)^2 + 4$

R $y = \dfrac{1}{x}$

S $4x + 3y = 12$

T $y = x^3 - 6x^2 + 12x - 6$

(a) Write down the letter of the **graph** which is an example of

    (i) an exponential function   (1 mark)

C ✓

    (ii) a cubic function   (1 mark)

D ✓

(b) Write down the letter of the **equation** which is an example of

    (i) a quadratic function   (1 mark)

Q ✓

    (ii) a reciprocal function   (1 mark)

R ✓

(c) Give the coordinates of

    (i) the y-intercept of the linear function   ✓   (1 mark)

Function is S. When $x = 0$, then $3y = 12 \Rightarrow y = 4$. Hence (0, 4).

    (ii) the turning point of the parabola   ✓   (1 mark)

Function is Q. Turning point is (3, 4).

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Question 7 (6 marks)

(a) Consider the statement that 'the sum of two consecutive odd counting numbers is always divisible by four'.

(i) Systematically check this statement with three examples. (2 marks)

$1 + 3 = 4$

✓ one example

$3 + 5 = 8$

✓ at least 2 examples

$5 + 7 = 12$

4, 8 and 12 are all divisible by 4.

(ii) Do your examples suggest that the statement is true or false? (1 mark)

True ✓

(b) Consider the statement that 'the sum of three consecutive terms of the Fibonacci sequence is always a multiple of six'.

(i) Systematically check this statement. (2 marks)

Fibonacci numbers are 1, 1, 2, 3, 5, ...

$1 + 1 + 2 = 4$ ✓

This first example is not a multiple of 6, so no need for more checking. ✓

(ii) Is the statement true or false? (1 mark)

False ✓

End of questions

Additional working space

Question number: _____